AN INTRODUCTION TO USING MATLAB

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Introduction

MATLAB is a software package for mathematical calculations. It is a very powerful package, but is also very simple to use. One of the attractions of MATLAB is its versatility. You can use it interactively or use it like a programming language. It can handle every think from a simple expression to a set of complex mathematical calculations on large sets of data. There is a massive number of predefine functions to choose from. There is also a large selection of simple to use graphics functions to plot and display data to the screen.

The purpose of this document is to introduce the fundamentals of MATLAB. After reading this document you should have a good idea of the type of problems that MATLAB can cope with and how to solve those problems. The document is designed for people that have never used MATLAB before. It is not the intention of this document to be a complete guide to MATLAB. It covers only a small fraction of the hundreds of commands available within MATLAB. However it does show you how to use the basic MATLAB commands and functions. It also explains how to use the help in MATLAB to find out what is available.
Starting MATLAB

Normally when MATLAB is installed a MATLAB icon is installed onto the desktop. Double click on the icon to start MATLAB.

If there is no MATLAB icon on the desktop, then MATLAB can be started in other ways. On a PC, select the following in turn :-

Start
   All Programs
       MATLAB
           R2018a
       MATLAB R2018a

On Linux and MAC, open a terminal window and enter the command
matlab

By now you should have a MATLAB window open in front of you.

The exact layout of the subwindows does vary from version to version. It is also possible to change the layout, so the appearance may be different from the picture above. However, it should be fairly easy to find the Command Window, which is normally the largest window. Don’t worry about the other windows for the time being. You will be shown how to use them later. We are going to start by entering commands into the command window.
Simple Expressions

To start with try entering the following simple expressions into the command window. The double arrow on the left (>>) is the MATLAB prompt and will appear after you have entered each expression. Enter the three expressions pressing return after each of the expressions.

```matlab
>> 1 + 2
>> 5^2
>> 7^2 + 5*7 -3
```

I suspect you have realized that you have just carried out the following calculations.

\[
\begin{align*}
1 + 2 &= 3 \\
5^2 &= 25 \\
7^2 + 5 \times 7 - 3 &= 81
\end{align*}
\]

The basic mathematical operators are

<table>
<thead>
<tr>
<th>Operation</th>
<th>Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>Addition</td>
<td>+</td>
</tr>
<tr>
<td>Subtraction</td>
<td>-</td>
</tr>
<tr>
<td>Multiplication</td>
<td>*</td>
</tr>
<tr>
<td>Division</td>
<td>/</td>
</tr>
<tr>
<td>Raise to a power</td>
<td>^</td>
</tr>
</tbody>
</table>

The order of precedence is that powers are evaluated first, followed by multiplication and division, with addition and subtraction last. Round brackets can be used to change the order of precedence. Calculations within brackets take precedence over everything else.

```matlab
>> (1 + 2)^2
ans =
9
```

When there are two items with the same level of precedence, the order is from left to right.

```matlab
>> 12/3*4
```

This means \( \frac{12}{3} \times 4 \) and not \( \frac{12}{3} \times 4 \) because the division operation is to the left of the multiplication operation.
Assignments

An assignment takes the value of an expression and stores it in a variable. For example:

```matlab
>> x = 1 + 2
>> a = 5^2
>> y = 7^2 + 5*7 -3
```

Once a variable has been created, you can use them in expressions.

```matlab
>> x^2
>> y = x^2 + 5*x -3
```

The first character of a variable name must be a letter. Other characters may be numbers or underscores. The variable name has a maximum length of 63 characters.

If you do not assign an expression to a variable, it is automatically assigned to a variable called “ans”, which can be used in subsequent expressions.

You may have noticed that each time you enter an expression; the result is printed in the command window. This is not always desirable. For example, the expression may be in a program where you don’t want to print intermediate results. Later we will be using arrays and matrices. Results from these calculations may cover several pages. To suppress the result being printed out, place a semicolon at the end of an expression. For example:

```matlab
>> x = 1 + 2 ;
>> a = 5^2 ;
>> y = 7^2 + 5*7 -3;
```

Output Display Format

The format command is used to change the way in which numbers are displayed.

- `format short` 5 digit floating point. The default.
- `format` Same as above.
- `format short e` 5 digit scientific notation.
- `format long` 15 digit floating point.
- `format long Ee` 15 digit scientific notation.
Mathematical Functions

There are hundreds of functions in MATLAB. To get started consider the standard mathematical functions that you would expect to find on a calculator.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>abs(x)</td>
<td>The absolute value or complex magnitude.</td>
</tr>
<tr>
<td>sqrt(x)</td>
<td>The square root.</td>
</tr>
<tr>
<td>round(x)</td>
<td>The value rounded to the nearest integer.</td>
</tr>
<tr>
<td>rem(x,b)</td>
<td>The remainder of x divided by b.</td>
</tr>
<tr>
<td>sin(x)</td>
<td>The sine.</td>
</tr>
<tr>
<td>cos(x)</td>
<td>The cosine.</td>
</tr>
<tr>
<td>tan(x)</td>
<td>The tangent.</td>
</tr>
<tr>
<td>asin(x)</td>
<td>The arcsine. The inverse of sin(x)</td>
</tr>
<tr>
<td>acos(x)</td>
<td>The arccosine.</td>
</tr>
<tr>
<td>atan(x)</td>
<td>The arctangent.</td>
</tr>
<tr>
<td>exp(x)</td>
<td>The exponential base e.</td>
</tr>
<tr>
<td>log(x)</td>
<td>The natural logarithm. ie to the base e</td>
</tr>
<tr>
<td>log10(x)</td>
<td>The log base 10.</td>
</tr>
</tbody>
</table>

Trigonometric functions all use radians. However, there are degree based versions of each of the functions. Their name is the same as the functions above, except for and extra "d" at the end of the name.

```
>> sind(45)
```

Functions can be used in any expression in any place you could put a number or a variable.

```
>> sin(x)^2 + cos(x)^2
>> 10^(log10(3) + log10(4))
```

The argument of a function (x and b in the table above) can also be an expression.

```
>> r = sqrt(3^2 + 4^2)
```

The argument can also contain calls to other functions.

```
>> exp(2*log(3) + 3*log(2))
```
Special Number Symbols

There are symbols in MATLAB that are used to indicate special numbers.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>pi</code></td>
<td>π</td>
</tr>
<tr>
<td><code>inf</code></td>
<td>∞</td>
</tr>
<tr>
<td><code>NaN</code></td>
<td>Not a number</td>
</tr>
</tbody>
</table>

There are also the symbols used in complex calculations.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>i</code></td>
<td>(\sqrt{-1})</td>
</tr>
<tr>
<td><code>j</code></td>
<td>(\sqrt{-1})</td>
</tr>
</tbody>
</table>

Mathematicians use \(i\) to represent the square root of minus one while in electronics they prefer to use \(j\). In the next section we will be looking at how to use MATLAB to carry out complex calculations.

Complex Numbers

Complex numbers can be entered in either Cartesian or polar form.

```matlab
>> z = 3 + 4i
>> w = 5 * exp(i * pi/6)
```

or

```matlab
>> w = 5*(cos(pi/6)+j*sin(pi/6))
```

Complex arithmetic is carried out with the normal arithmetic operators. MATLAB automatically detects if a calculation contains complex numbers and carries out the appropriate calculation.

There are also functions that allow you to obtain particular properties of the complex number.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>real(A)</code></td>
<td>The real part of A</td>
</tr>
<tr>
<td><code>imag(A)</code></td>
<td>The imaginary part of A</td>
</tr>
<tr>
<td><code>conj(A)</code></td>
<td>The complex conjugate of A</td>
</tr>
<tr>
<td><code>abs(x)</code></td>
<td>The modulus of A.</td>
</tr>
<tr>
<td><code>angle(A)</code></td>
<td>The phase angle of A</td>
</tr>
</tbody>
</table>
Matrices

The fundamental unit of MATLAB is a matrix. In fact MATLAB is short for matrix laboratory. However, its use is not restricted to matrix mathematics. Matrices in MATLAB can also be regarded as arrays of numbers. You can regard matrices as a convenient way of handling groups of numbers. A matrix in MATLAB can have one, two or more dimensions or be empty. A matrix with a single element is a special case. They are treated as a single number. A matrix element can be an integer, a real or a complex number. You do not have to worry about element types. MATLAB will set the element type to what is required. Matrices that contain a single row or column are called vectors.

\[
\begin{bmatrix}
1 & 5 & 7 & 8.8 & 7.42 \\
4.6 & 72 & 5i & 92 & 44 \\
7i & 65 & 77 & 63 & 4.2 \\
3 + 5i & 22 & 4.11 & 54 & 54 \\
17.3 & 111 & 32 & 21 & 21 \\
83.2 & 230 & 12 & 4i & 16
\end{bmatrix}
\]

\[
\begin{bmatrix}
12 \\
18 \\
8.8 \\
17 \\
5 \\
1.01
\end{bmatrix}
\]

Matrix

\[
\begin{bmatrix}
12 & 15 & 2i & -17 & 3.89
\end{bmatrix}
\]

Row Vector

\[
34.2
\]

Column Vector

When specifying the position of an element or the size of a matrix, the convention is to specify the row before the column. To remember this, I remember R before C like in “Roman Catholic”. 
Entering Matrices

To enter the contents of a matrix:

Enclose the contents in square brackets.
Separate each element by white space or a comma.
Separate each row by a semicolon or a new line.

Here are various ways of entering into a matrix containing

\[
\begin{bmatrix}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9
\end{bmatrix}
\]

\[
>> x = [ 1, 2, 3; 4, 5, 6; 7, 8, 9]
\]

\[
>> x = [ \begin{array}{ccc}
1 & 2 & 3 \\
4 & 5 & 6 \\
7 & 8 & 9 
\end{array}
\]

\[
>> a = [ 1 \ 2 \ 3 ]
\]

\[
>> b = [ 4 \ 5 \ 6 ]
\]

\[
>> c = [ 7 \ 8 \ 9 ]
\]

\[
>> x = [ a \ ; \ b \ ; \ c ]
\]

\[
>> x = [ 1, 2 3 \\
b ; c]
\]

You can increase the size of a matrix by adding rows or columns.
For Example:

\[
>> x = [ x \ ; 10 \ 11 \ 12]
\]

When adding a row to matrix, the number of elements in the additional row must be the same as the number of elements in each row of the matrix. The same is true for columns.

When you enter a matrix, each of the elements can be entered as an expression.

\[
>> a = [ \text{exp}(0) \ \text{sqrt}(4) \ 1+2 ]
\]
Matrix Operations

These operations treat each of the operands as a matrix:

- Matrix Addition
- Matrix Subtraction
- Matrix Multiplication
- Right Matrix Division
- Left Matrix Division
- Raise to a power
- Transpose matrix

To understand what is going on, let's look at some examples.

```
>> A = [ 1 2 ; 3 4];
>> B = [ 5 6 ; 7 8];
```

This produces two matrices that we can use in the examples.

\[
A = \begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix}
\quad \quad
B = \begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix}
\]

```
>> A + 5
```

This adds 5 to each element of A.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} + 5 = \begin{bmatrix}
1+5 & 2+5 \\
3+5 & 4+5
\end{bmatrix} = \begin{bmatrix}
6 & 7 \\
8 & 9
\end{bmatrix}
\]

```
>> A + B
```

This adds each element of A to the corresponding element in B.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} + \begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix} = \begin{bmatrix}
1+5 & 2+6 \\
3+7 & 4+8
\end{bmatrix} = \begin{bmatrix}
6 & 8 \\
10 & 12
\end{bmatrix}
\]

```
>> A - B
```

This subtracts each element of B from the corresponding element in A.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} - \begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix} = \begin{bmatrix}
1-5 & 2-6 \\
3-7 & 4-8
\end{bmatrix} = \begin{bmatrix}
-4 & -4 \\
-4 & -4
\end{bmatrix}
\]
>> A * 5

This multiplies each element in A by 5

\[
\begin{bmatrix}
1 & 2 \\
3 & 4 \\
\end{bmatrix} \times 5 = \begin{bmatrix}
1\times5 & 2\times5 \\
3\times5 & 4\times5 \\
\end{bmatrix} = \begin{bmatrix}
5 & 10 \\
15 & 20 \\
\end{bmatrix}
\]

>> A * B

Multiply matrix A by B.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4 \\
\end{bmatrix} \times \begin{bmatrix}
5 & 6 \\
7 & 8 \\
\end{bmatrix} = \begin{bmatrix}
1\times5 + 2\times7 & 1\times6 + 2\times8 \\
3\times5 + 4\times7 & 3\times6 + 4\times8 \\
\end{bmatrix} = \begin{bmatrix}
19 & 22 \\
43 & 50 \\
\end{bmatrix}
\]

>> A ^ 2

Multiply matrix A by itself.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4 \\
\end{bmatrix} \times \begin{bmatrix}
1 & 2 \\
3 & 4 \\
\end{bmatrix} = \begin{bmatrix}
1\times1 + 2\times3 & 1\times2 + 2\times4 \\
3\times1 + 4\times3 & 3\times2 + 4\times4 \\
\end{bmatrix} = \begin{bmatrix}
7 & 10 \\
15 & 22 \\
\end{bmatrix}
\]

>> A'

Transpose matrix A. Swap rows with columns.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4 \\
\end{bmatrix}^{\prime} = \begin{bmatrix}
1 & 3 \\
2 & 4 \\
\end{bmatrix}
\]
Matrix Division

Matrix division is not something that you find in normal mathematical textbook. As you would expect, matrix division is the inverse of matrix multiplication. What is not so obvious is that matrix division is the same as solving a set of simultaneous equation. For example, take the pair of equations:

\[ \begin{align*}
    x_1 + 2x_2 &= 5 \\
    3x_1 + 4x_2 &= 11
\end{align*} \]

In matrix form this becomes:

\[ \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 5 \\ 11 \end{bmatrix} \]

\[ Ax = b \]

Where \( A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \), \( x = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \) and \( b = \begin{bmatrix} 5 \\ 11 \end{bmatrix} \)

If you multiply both sides by \( A^{-1} \) (the inverse matrix of A).

\[ A^{-1}Ax = A^{-1}b \]

\[ x = A\backslash b \]

In MATLAB you enter:

\[
\begin{align*}
\text{>> A} &= \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} ; \\
\text{>> b} &= \begin{bmatrix} 5 \\ 11 \end{bmatrix} ; \\
\text{>> A\backslash b} &
\end{align*}
\]

You need to be careful because matrix multiplication is not commutative. That is to say in general \( A \times B \) does not equal \( B \times A \). That is why there are two division operators.

<table>
<thead>
<tr>
<th><strong>Left Division</strong></th>
<th><strong>Right Division</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td>( A\backslash b = A^{-1}b )</td>
<td>( b / A = bA^{-1} )</td>
</tr>
<tr>
<td>Divide b by A.</td>
<td>Divide b by A.</td>
</tr>
<tr>
<td>The divide is to the left of b.</td>
<td>The divide is to the right of b.</td>
</tr>
</tbody>
</table>
Array Operations

These operations act on corresponding pairs of elements in each of the operands. To distinguish them from the matrix operations, each is preceded by a dot.

<table>
<thead>
<tr>
<th>Array Multiplication</th>
<th>.*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Right Array Division</td>
<td>./</td>
</tr>
<tr>
<td>Left Array Division</td>
<td>.\</td>
</tr>
<tr>
<td>Raise to a power</td>
<td>.^</td>
</tr>
</tbody>
</table>

The operands must be the same size, unless one of the operands is a single number. You may want to compare the following examples with the examples of matrix operations.

```matlab
>> A .* B
Multiply each element in A by the corresponding element in B.

\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} \times \begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix} = \begin{bmatrix}
5 \times 1 & 2 \times 6 \\
3 \times 7 & 4 \times 8
\end{bmatrix} = \begin{bmatrix}
5 & 12 \\
21 & 32
\end{bmatrix}
\]

```matlab

>> A ./ B
Divide each element in A by the corresponding element in B.

```matlab
\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} \div \begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix} = \begin{bmatrix}
1 \div 5 & 2 \div 6 \\
3 \div 7 & 4 \div 8
\end{bmatrix} = \begin{bmatrix}
0.2 & 0.3333 \\
0.4286 & 0.5
\end{bmatrix}
\]

```matlab

Array operations are commutative. Therefore A./B = B.\A

```matlab
>> A .^ 2
Square each element in A

```

```matlab
\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} ^2 = \begin{bmatrix}
1^2 & 2^2 \\
3^2 & 4^2
\end{bmatrix} = \begin{bmatrix}
1 & 4 \\
9 & 16
\end{bmatrix}
\]

```matlab

```matlab
>> A .^ B
Raise each of the elements in A to the power of the corresponding element in B.

```

```matlab
\[
\begin{bmatrix}
1 & 2 \\
3 & 4
\end{bmatrix} ^\begin{bmatrix}
5 & 6 \\
7 & 8
\end{bmatrix} = \begin{bmatrix}
1^5 & 2^6 \\
3^7 & 4^8
\end{bmatrix} = \begin{bmatrix}
1 & 64 \\
2187 & 65536
\end{bmatrix}
\]

```
Matrices and Functions

If you apply an arithmetic function to a matrix, then the function is applied to each of the elements in the matrix.

\[
\text{>> sqrt}(A) \\
\text{The square root of each element in A}
\]

\[
\text{sqrt} \left(\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \right) = \begin{bmatrix} \sqrt{1} & \sqrt{2} \\ \sqrt{3} & \sqrt{4} \end{bmatrix}
\]

\[
\text{>> sin}(A) \\
\text{The sine of each element in A}
\]

\[
\text{sin} \left(\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \right) = \begin{bmatrix} \sin(1) & \sin(2) \\ \sin(3) & \sin(4) \end{bmatrix}
\]

\[
\text{>> exp}(A) \\
\text{The exponent of each element in A}
\]

\[
\text{exp} \left(\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \right) = \begin{bmatrix} e^1 & e^2 \\ e^3 & e^4 \end{bmatrix}
\]

However there are functions that act on the whole matrix. They are only defined for square matrices.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>sqrtm(x)</td>
<td>The matrix square root.</td>
</tr>
<tr>
<td>expm(x)</td>
<td>The matrix exponential base e.</td>
</tr>
<tr>
<td>logm(x)</td>
<td>The matrix natural logarithm.</td>
</tr>
</tbody>
</table>
Help

There are over a thousand different functions in MATLAB and many more in additional toolboxes. So the ability to find the function you need and learn how to use it is a very important to MATLAB users. Fortunately there are many ways of finding help, the most important of which are mentioned below.

Command line help

In the command line you can just enter help and the name of the function.

    >> help log
    >> help exp

A description of the function and how to use it will be printed in the command window. The problem with the help command is that you don't always know the name of the function you are looking for. In that case, you use the lookfor command.

    >> lookfor average

If you do this you will find that there is a function call mean that returns the average. You can then use the help command to find out how to use mean.

    >> help mean

There are also hundreds of demo programs on the system that you can use for inspiration. To see them enter demo in the command window.

    >> demo
The Help menu

Everything that is in the command line help and much more is available in the MATLAB documentation. To see the documentation, click on the question mark icon on the home banner.

Then click on MATLAB.

You can search the documentation by clicking on the Search Documentation text and entering what it is you want to search for, then click on the blue magnifying glass.

Click on the contents icon a few times to see what it does.
Utility Matrices
These functions are used to create standard matrices.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>zeros(n)</td>
<td>n by n matrix where each element is zero.</td>
</tr>
<tr>
<td>zeros(m,n)</td>
<td>m by n matrix where each element is zero.</td>
</tr>
<tr>
<td>ones(n)</td>
<td>n by n matrix where each element is one.</td>
</tr>
<tr>
<td>ones(m,n)</td>
<td>m by n matrix where each element is one.</td>
</tr>
<tr>
<td>rand(n)</td>
<td>n by n matrix of random numbers.</td>
</tr>
<tr>
<td>rand(m,n)</td>
<td>m by n matrix of random numbers.</td>
</tr>
<tr>
<td>eye(n)</td>
<td>n by n identity matrix.</td>
</tr>
</tbody>
</table>

Generating Vectors
It is often useful to produce a row vector (a matrix containing only one row) containing a sequence of numbers. A colon can be used to produce a sequence containing two integers and all the integers in between.

```
>> x = 1 : 5                                       generates a row vector x = [ 1 2 3 4 5 ]
```

A third term in between the other two can be used to specify the gap between each number.

```
>> w = 0:0.25:1                                     generates w = [0 0.25 0.5 0.75 1]
>> y = 0:5:20                                       generates y = [0 5 10 15 20]
>> z = 6:-1:1                                       generates z = [6 5 4 3 2 1]
```

There are also functions that can generate vectors. The function linspace produces a vector with a specified number of elements.

```
>> y = linspace(start,end,n)
```

This produces an evenly spaced vector with n elements. The first element is “start”, the last is “end”.

```
>> y = linspace(0,10,5)                              generates y = [0 2.5 5 7.5 10]
```

The function logspace produces a vector with a logarithmic distribution.

```
>> y = logspace(d1,d2,n)
```

This generates a row vector with n elements logarithmically spaced between $10^{d1}$ and $10^{d2}$.

```
>> y = logspace(-1,2,4)                              generates y = [0.1 1 10 100]
```
Subscripts

Subscripts are used to access individual elements of a matrix or produce a sub matrix from a matrix. They can be used to assign a value to an element or to read the contents of an element. As an example, consider the matrix $A$.

$$A = \begin{bmatrix}
1 & 2 & 3 & 4 \\
5 & 6 & 7 & 8 \\
9 & 10 & 11 & 12
\end{bmatrix}$$

An individual element can be read or written to by specifying the row and column in parentheses after the variable name. To read the element in the second row and third column of $A$, you would write:

```matlab
>> A(2,3)
```

This would return 7. To change the 7 to 100 you could enter:

```matlab
>> A(2,3)=100;
```

Multiple elements can be accessed at a time. A vector can be used to specify a range of rows or columns.

```matlab
>> A(2,[1 2 4])
```

Returns $[5 \ 6 \ 8]$

Vector notation can be used to specify the range.

```matlab
>> A(1:2,3)
```

Returns $[3 \ 7]$

A colon is used to specify every element of the corresponding row or column.

```matlab
>> A(3,:)
```

Returns $[9 \ 10 \ 11 \ 12]$
If you use subscripting on a vector, then you only need to specify one dimension.

```matlab
>> B=10:15
  [10 11 12 13 14 15]
>> B(2)
  Returns 11
  [10 11 12 13 14 15]
>> B([2,4])
  Returns [11 13]
  [10 11 12 13 14 15]
>> B(4:end)
  Returns [13 14 15]
  [10 11 12 13 14 15]
```

You can also use the result of a comparison as a subscript. Suppose that we want to find all numbers in B that are greater than 13. First we compare B with 13.

```matlab
>> p = B > 13
  Returns [0 0 0 1 1]
```

Here a one indicates that the comparison is true. In this case, the elements of B that are greater than 13. A zero indicates that the comparison is false.

Now p can be used as a subscript, to extract all elements where the comparison is true.

```matlab
>> B(p)
  Returns [14 15]
  [10 11 12 13 14 15]
```

### Relational and Logical Operations

As we have seen above, we can compare a number with each element in a matrix. You can also compare pairs of corresponding elements in two matrices of equal dimensions.

The result is a matrix of zeros and ones. They return one for TRUE, or zero for FALSE.

<table>
<thead>
<tr>
<th>relational operator</th>
<th>syntax</th>
</tr>
</thead>
<tbody>
<tr>
<td>Less than</td>
<td><code>&lt;</code></td>
</tr>
<tr>
<td>Less than or equal</td>
<td><code>&lt;=</code></td>
</tr>
<tr>
<td>Greater than</td>
<td><code>&gt;</code></td>
</tr>
<tr>
<td>Greater than or equal</td>
<td><code>&gt;=</code></td>
</tr>
<tr>
<td>Equal</td>
<td><code>==</code></td>
</tr>
<tr>
<td>Not equal</td>
<td><code>~=</code></td>
</tr>
</tbody>
</table>

Once you have the results of such an operation, you can carry out Boolean logic operations on them.

<table>
<thead>
<tr>
<th>logical operator</th>
<th>syntax</th>
</tr>
</thead>
<tbody>
<tr>
<td>AND</td>
<td><code>&amp;</code></td>
</tr>
<tr>
<td>OR</td>
<td>`</td>
</tr>
<tr>
<td>NOT</td>
<td><code>~</code></td>
</tr>
</tbody>
</table>
Variable Control Commands

<table>
<thead>
<tr>
<th>Command</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>who</td>
<td>List all variables in memory.</td>
</tr>
<tr>
<td>whos</td>
<td>Same as above but with more information.</td>
</tr>
<tr>
<td>clear</td>
<td>Remove all variables from memory.</td>
</tr>
<tr>
<td>clear &lt;variable&gt;</td>
<td>Remove specified variables from memory.</td>
</tr>
</tbody>
</table>

For example

```matlab
>> x = 1; y = 2; z = 3;
>> who
Name         Size       Bytes  Class  Attributes
x             1x1        8       double
y             1x1        8       double
z             1x1        8       double
```

```matlab
>> clear x  y;
>> who
Name         Size       Bytes  Class  Attributes
z             1x1        8       double
```

File Control Commands

<table>
<thead>
<tr>
<th>Command</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>dir</td>
<td>List contents of current directory.</td>
</tr>
<tr>
<td>ls</td>
<td>List contents of current directory.</td>
</tr>
<tr>
<td>what</td>
<td>List the Matlab files in the current directory.</td>
</tr>
<tr>
<td>cd &lt;directory&gt;</td>
<td>Change the current directory.</td>
</tr>
<tr>
<td>type &lt;filename&gt;</td>
<td>Display the contents of a text or .m file.</td>
</tr>
<tr>
<td>delete &lt;filename&gt;</td>
<td>Delete a file.</td>
</tr>
<tr>
<td>diary &lt;filename&gt;</td>
<td>Record all commands and results to a file.</td>
</tr>
<tr>
<td>diary off</td>
<td>Stop above.</td>
</tr>
</tbody>
</table>
Saving, Exporting and Importing Data

MATLAB can load and save data in several different file formats. It has its own binary data format that can only really be understood by MATLAB. Files of this type have a ".mat" extension. It can also use ascii text files. These are files containing numbers written in the standard ASCII text, like you would produce in note pad or a text editor. Columns are separated with white space and each row is on a separate line. MATLAB will also read and write comma separated value(.csv) files.

<table>
<thead>
<tr>
<th>Command</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>save</td>
<td>Save all variable to the file matlab.mat</td>
</tr>
<tr>
<td>load</td>
<td>Load in variables from the file matlab.mat</td>
</tr>
<tr>
<td>save &lt;filename&gt;</td>
<td>Save all variable to the file filename.mat</td>
</tr>
<tr>
<td>load &lt;filename&gt;</td>
<td>Load in variables from the file filename.mat</td>
</tr>
<tr>
<td>save &lt;filename&gt; &lt;variable&gt;</td>
<td>Save only the variable variable to the file filename.mat</td>
</tr>
<tr>
<td>load &lt;filename&gt; &lt;variable&gt;</td>
<td>Load in only the variable variable from the file filename.mat</td>
</tr>
<tr>
<td>save &lt;filename&gt; &lt;variable&gt; -ascii</td>
<td>Save variable to the text file filename</td>
</tr>
<tr>
<td>load &lt;filename&gt;.&lt;ext&gt;</td>
<td>Load from the text file, to a variable called filename</td>
</tr>
<tr>
<td>save &lt;filename&gt; &lt;variable&gt; -ascii -double</td>
<td>Save variable to the text file filename using double precision.</td>
</tr>
<tr>
<td>csvwrite(&lt;filename&gt;.csv , M)</td>
<td>Write matrix M to csv file.</td>
</tr>
<tr>
<td>M=csvread( &lt;filename&gt;.csv)</td>
<td>Load from the csv file, into variable M</td>
</tr>
</tbody>
</table>

Matlab can also read in other file formats. For more information, enter

```
doc 'Supported File Formats'
```

in the command window.
The Desktop

Almost anything you want to do in MATLAB can be done from the Command Window. However, there are numerous other windows that can make certain procedures simpler. If you look at the MATLAB window on a computer, it will look something like this.

You can drag windows around, remove them and resize them. The MATLAB layout is like a Rubik’s cube, three moves and it is very difficult to get back to where you started. However, you can always select Layout ► Default on the banner, under the Home tab.

Command History

This shows all the previous commands that you have entered in the command window. Double clicking on a command in this window will execute the command. You can also drag the command back into the command window, edit them and run them again. Another way of doing this is to use the up and down cursor keys in the command window to recall previous commands. You can then use the left and right cursor keys and the delete key to edit the command.

You can also use the Command History to create a program file. Hold down the ctrl key and click on each of the commands that you want in the file. Then right click and select Create Script. The selected commands will be copied into the MATLAB editor.
Workspace
The Workspace window is a variable explorer. Clicking on a variable with the right mouse button allows you to rename or delete a variable. If you double click on a variable, it opens a Variables Editor that allows you to change the contents of a variable.

Current Folder
Like most operating systems, MATLAB uses the concepts of a path and a current directory (folder). The path is a list of directories where MATLAB will search for files. The path is set when you install MATLAB to include all the necessary directories in the MATLAB installation. MATLAB also includes the current folder in the search path. While it is possible to add directories to the path (See Search Path in MATLAB help) the most common way of ensuring that MATLAB can see your files is to change the current folder to the required location.

To change the current directory(folder), you can use the cd command, like you would in windows, Linux or OSX. However, I find the box at the top of the MATLAB window more convenient to use.

Associated with this is the Current Folder Window. This window is like a file manager or windows explorer.

- Double clicking on a .m file will open the file in the MATLAB editor.
- Double clicking on a .mat file will load the variables stored in the file.
- Double clicking on a folder will set the current directory to that folder.
- Double clicking on a Excel file will open the file import window.

You can create new files and folders by right clicking on the window background.

If you right click on a file or folder, you can select to rename or delete the file or folder. You can also use this method to run a MATLAB program or import data from a file.
MATLAB as a Programming Language

So far we have treated MATLAB like a super calculator. However, every command and expression we have used so far can be used in a MATLAB program. In this sense the commands and expressions of MATLAB can be regarded as a programming language. MATLAB has all the constructs you would expect in a programming language, such as loops, functions and conditional execution. These programs are stored in files with a ".m" suffix. For this reason they are generally called M files. There are two types of M files, scripts and functions.

Script M Files

A MATLAB script is a file containing a list of MATLAB commands. The commands in the script are executed by entering the name of the file without the ".m" suffix. The easiest way to create an M file is to use the editor. Try the following. At the matlab prompt enter

```
>> edit myscript.m
```

In the editor, enter

```
x = linspace(0,2*pi,100);
y = sin(x);
plot(x,y);
```

Then save. At the matlab prompt enter the name of the script to run it.

```
>> myscript
```

You can add your own comments to the script. Place a percent sign (%) before each comment. Everything after the percent sign on that line is regarded as a comment. Comments are displayed in green in the editor.

You may find these functions and commands useful within a script.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>A = input( 'What is A ?');</td>
<td>Ask the user for a number.</td>
</tr>
<tr>
<td>pause</td>
<td>Wait for the user to press a key.</td>
</tr>
<tr>
<td>pause(5)</td>
<td>Wait for 5 seconds</td>
</tr>
<tr>
<td>! command</td>
<td>Execute and operating system command</td>
</tr>
<tr>
<td>display(a)</td>
<td>Suppose a = 5. This would print &quot;a = 5&quot;;</td>
</tr>
<tr>
<td>disp(a)</td>
<td>Same as above, but with out the &quot;a = &quot;.</td>
</tr>
</tbody>
</table>
Function M Files

If an M file has the word "function" on the first line, then the file contains a definition of a MATLAB function. Here is a listing of a file called corner.m.

```matlab
function y = corner(x)
% CORNER the corners of a matrix.
% corner(x) returns a two by two matrix containing the values
% in each of the four corners of x.
[n,m]=size(x);    % The number of rows and columns of x
y = [ x(1,1) x(1,m) ; x(n,1) x(n,m) ];
```

The first line specifies that the function name is "corner" and that "x" is an input parameter and "y" is the return value. The next three lines are comments. These lines are used by the help command, they will be printed out if you type "help corner". The rest of the file contains the commands to implement the function. The last line assigns a value to "y" which is returned. The variable "n" and "m" are local to the function. They cannot be accessed outside the function. This function can now be used in an expression in the same way as any other function.

```matlab
>> corner(p)
>> c = corner(w);
>> help corner
```

You may have noticed that we used a function called size. This returned the number of rows and the number of columns of the matrix x. Unlike some programming languages, MATLAB functions can return more that one item. The following example shows how you would write a function that returns many items.

```matlab
function [sum,difference] = add_subtract(a,b)
sum = a + b;
difference = a - b;
```

To call this function, you would enter :-

```matlab
>> [s d] = add_subtract(1,2)
```

The variable "s" contains the sum, and "d" the difference.
Flow Control
So far, all the programs have consisted of lines of statements carried out in sequential order. However, most programs will need to be able to select conditionally which instructions to execute and repeat part of the program several times by using a loop. MATLAB has enumerated loops (for loops), precondition loops (while loops) and conditional execution (if statements).

Enumerated Loops (for)
Enumerated loops are used to repeat a sequence of statements a known number of times.

```matlab
for x = 1:10
    y(x) = x.^2+3*x+5;
end
```

The middle line is the statement to be repeated. Here it is only one line, but it could just as easily be several lines. Any line between for and end is repeated. The loop is repeated for each item in an enumerated sequence. In this case the sequence is the numbers one to ten. Each time around the loop, the loop counter variable "x" is assigned one of the numbers in the sequence, in order. So the first time around the loop, "x" will be one, the next time around the loop it will be two, then three, then four, up to ten.

In most programming languages, the enumerated sequence is defined by stating a rule for finding the next number in the sequence. The enumerated sequence in MATLAB is defined by a vector. Which means you can use a sequence with no logical connection between items in the sequence.

```matlab
A = rand(1,5);
for a = A
    disp(a)
end

for k = [ 1 7 3 pi i]
    disp(k)
end
```

The general form of a for loop is :-

```matlab
for <variable> = < vector>
    <statement>
    <statement>
    etc
end
```

New MATLAB users, especially those that have experience of computer programming, tend to over use for loops. The first example can be achieved much more efficiently without using a loop at all.

```matlab
>> x = 1:10
>> y = x.^2+3*x+5;
```
**Precondition Loops (while)**

A precondition loop is used to repeat a sequence of statements zero, one or more times. Unlike the enumerated loop, the number of repetitions is not a fixed quantity and can change as the loop runs.

The following example shows how to use a precondition loop to implement an iterative process.

```plaintext
A = 7;  %Want to find the square root of A.
x = 1;  %First guess
err = 1;  %Set error to something to get started

while (err > 0.0001)
    x = (x.^2 + A) / (2*x);  %Iteration equation (Newton Raphson)
    err = abs(A - x.^2);  %calculate the error
end

disp(x);
```

The loop consists of all the statements in the lines between while and end. The condition in the brackets to the right of while determines if the loop is going to execute or not. First the condition is evaluated. If the result is true (non zero) then the two lines below the while are executed. The program then goes back to the start of the while loop and evaluates the condition again. The loop will keep repeating until the result of the condition evaluates to false (zero). When this happens the lines between while and end are not executed. The program jumps to the first line after the end.

Below is the general form of a **while** loop.

```plaintext
while (<condition>)
    <statement>
    <statement>
    etc
end
```

You loop **while** the condition is true.

You can put in as many statements as you like in the loop. The loop can include other while loops, for loops and if statements.
Conditional Execution (if)

The if statement is very like a while loop, except that it will only run once if at all.

```
if(<condition>)
  <statement>
  <statement>
  etc
end
```

If the condition is true, the statements inside are executed. They will not be executed if the condition is false. In either case, the if statement is then finished and the program goes to the next line in the program. The following example finds the absolute value of the variable A.

```
if (A<0)  % If A is negative
  A = -A;  % Make A Positive
end
```

There is another form of if statement

```
if(<condition>)
  <statement>
  <statement>
  etc
else
  <statement>
  <statement>
  etc
end
```

If the condition is false, the statements after the else are executed.

For example

```
if (A<B)  % If A is negative
  disp('A is less than B')
else
  disp('A is not less than B')
end
```

You can put in as many statements in the conditional parts as you like. These can include while loops, for loops and other if statements.
Graph Commands

This section describes how you can produce graphs in MATLAB. The script below shows how to plot and annotate a simple graph.

```matlab
%% Matlab Script to plot a Sin Wave

%% Create the x and y vectors to plot
x = 0:6:360; % The values of x in degrees
rads = 2*pi*x./360; % The above convert to radians
y = sin(rads); % Calculate the values of y
plot(x,y); % Plot the graph

%% Annotate the graph
title('Sine Wave'); % Add a Title
xlabel('degrees'); % Label the x axis
ylabel('value'); % Label the y axis
grid; % Draw a grid on the graph
axis([0 360 -1 1]); % Set the limits of the x and y axis
```

Running this script produces the following graph
2D Graphics Commands

The plot command produces a linear x-y plot. Listed below is a selection of plot commands.

- **plot(y)**  
  Plot y against the element number.

- **plot(x,y)**  
  Plot y against x.

- **plot(x1,y1,x2,y2)**  
  Plot y1 against x1 and y2 against x2.

You can use a third argument to define various options.

- **plot(x,y,'r+')**  
  Plot y against x using red plus signs.

- **plot(x1,y1,'r+',x2,y2,'go')**  
  Use red plus signs for x1 and y1 and green circles for x2 y2.

Plot options are used to define the line type or point type and the colour. Plot options are enclosed in quotes to distinguish them from variables.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Point or Line Type</th>
<th>Symbol</th>
<th>Colour</th>
</tr>
</thead>
<tbody>
<tr>
<td>.</td>
<td>Points</td>
<td>y</td>
<td>Yellow</td>
</tr>
<tr>
<td>o</td>
<td>Circles</td>
<td>m</td>
<td>Magenta</td>
</tr>
<tr>
<td>x</td>
<td>X marks</td>
<td>c</td>
<td>Cyan</td>
</tr>
<tr>
<td>+</td>
<td>Plus Signs</td>
<td>r</td>
<td>Red</td>
</tr>
<tr>
<td>*</td>
<td>Stars</td>
<td>g</td>
<td>Green</td>
</tr>
<tr>
<td>-</td>
<td>Solid Line</td>
<td>b</td>
<td>Blue</td>
</tr>
<tr>
<td>:</td>
<td>Dotted Line</td>
<td>w</td>
<td>White</td>
</tr>
<tr>
<td>-.</td>
<td>Dash dot Line</td>
<td>k</td>
<td>Black</td>
</tr>
<tr>
<td>--</td>
<td>Dashed Line</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The plot options can be one, two or three characters long. For example 'rx-' will plot x marks and a solid line, both in red.

In addition to the plot command, there are other commands to produces other types of 2D graphs. On the next page are various examples of the graphs produced by the commands fill, bar, stairs, etc. The arguments and options of these commands are similar to those of plot.
**Subplots**

Subplot enables you to split the graphics window into a number of smaller subgraphs. As an example, consider how the graphs where plotted on the previous page.

```matlab
subplot(4,3,1); % 4 by 3 graphs, 1st graph
fill(degrees,sin(rad),'g'); % Plot a Fill graph
```

The subplot command has three arguments. The first digit specifies the number of rows of graphs you want and the second the number of columns. In this case we are going to have 4 rows of graphs in 3 columns. The third number specifies which of the 12 subgraphs you are going to use next. The subgraphs are numbered from left to right, top to bottom. So the Fill plot will be in the top left had corner. Next to it is the bar plot.

```matlab
subplot(4,3,2); % 4 by 3 graphs, 2nd graph
bar(degrees,sin(rad),'g'); % Plot a Bar Graph
```

and so on.

```matlab
subplot(4,3,3); % 4 by 3 graphs, 3rd graph
stairs(degrees,sin(rad)); % Plot a Stair Graph
subplot(4,3,4); % 4 by 3 graphs, 4th graph
```

e tc

**Figure**

An alternative to splitting a window into several graphs is to open a new window. MATLAB calls a graphics window a figure. To open a new figure, you use the `figure` command.

```matlab
figure; % Open a new window.
```

This opens a new figure, which becomes the current graphic window. Any subsequent plots will be drawn in the new figure. Figures are numbered 1,2,3 etc, which is called the handle. The `figure` command returns the handle of the new figure.

```matlab
h=figure; %h is the handle of the new figure.
```

The `figure` command can also be used to set the current figure to an existing figure.

```matlab
figure(h); %Set the current figure to h.
```

Here are some other commands that are useful for managing figures.

- `clf` Clear the current figure.
- `clf(h)` Clear figure h.
- `h = gcf` Get the handle of the current figure
- `delete(h)` Delete figure h.
**Hold**

The hold command enables you plot a graph over the top of another graph. In the default state, when a new graph is plotted, the old graph is removed first. The hold command stops the removal of the old graph. Any subsequent graphs are plotted on top of each other using the same axis.

- `hold on`: Hold the plot on the screen.
- `hold off`: Release the plot on the screen.
- `hold`: Toggle the hold state.

**Conclusion**

This seminar by necessity is fairly restricted. It has only covered a very small fraction of MATLAB commands and functions. If you want to get some idea of what else is in MATLAB, scroll through the function reference in Help. We have not even touched on any of the toolboxes. However, don't let that put you off. Very few people, if any body knows how to use all the functions within MATLAB. The seminar includes the fundamental basic commands and operations that you need to use the software. These should be sufficient to cover most, if not all of your requirements.

Although this seminar can only deal with the basics, it has a secondary aim of showing you ways of finding out more information. If you want to use some of the more specialized areas of MATLAB like Statistics, 3D graphics, graphical user interfaces, etc, I hope that you now have a better idea where you go to find out how to do it. On the next page you will find various links that can provide you with additional information.

You should now be able to use MATLAB interactively and to write your own functions and scripts, perhaps using this document as a reference. Like most skills, it is practise that is required. So I hope that you will go back to your own computer and start using it.
Further Information

If you want to know more about using MATLAB, always try looking in help first. In particular, there are links to video tutorials. You will find these at

http://uk.mathworks.com/help/index.html

The Oxford University MATLAB Portal
This is a one stop shop for MATLAB users in the University of Oxford.


MATLAB Academy Online Training Suite
This includes over 60 hours of online training courses for different levels and across different subject categories. See the MATLAB portal above.

MATLAB course at University of Oxford, IT Services
IT Services run a course called Matlab: A comprehensive introduction

https://help.it.ox.ac.uk/courses/overview

University Licences
For an overview of the various ways to license MATLAB within the University, see:

http://www.eng.ox.ac.uk/~labejp/TAH/matlabTAH.html